MATH 219 Introduction to Differential Equations

Credit: (4-0) 4

<u>Catalog description:</u> First order equations and various applications. Higher order linear differential equations. Power series solutions. The Laplace transform. Solutions of initial value problems. Systems of linear differential equations. Introduction to partial differential equations.

Course Objectives: By the end of this course, a student will:

- Classify and identify different types of differential equations,
- Explicitly solve several important classes of ordinary differential equations and interpret their qualitative behavior,
- Apply ideas from linear algebra in order to solve single linear ordinary differential equations and systems of such equations,
- Model certain physical phenomena using differential equations and reinterpret their solutions physically,
- Use power series methods to solve second order linear differential equations
- Apply the Laplace transform for solving differential equations,
- Use the method of separation of variables in order to solve some basic partial differential equations via Fourier series.

<u>Course Coordinator:</u> Özcan Yazıcı (Office: 127, Mathematics Department. Phone: (312) 210 5387 <u>oyazici@metu.edu.tr</u>

<u>Course Assistant:</u> İrem Özge Taşpınar (Office: Z-34, Mathematics Department. Phone: (312) 210 5365) isarac@metu.edu.tr

Course Website: http://ma219.math.metu.edu.tr/ and odtuclass.metu.edu.tr

<u>Textbook:</u> "Elementary Differential Equations and Boundary Value Problems", Boyce, W. E., DiPrima, R. C., 10^{th} ed.

Office Hours: To be announced.

Exams and Grading: The grading will be based on two midterm examinations and one final examination.

- **Midterm 1:** 30 % (November 15, Saturday at 13:30)
- **Midterm 2:** 30 % (December 20, Saturday at 13:30)
- **Final:** 40 % (January 8, Thursday at 13:30)

<u>Suggested Problems</u>: A list of suggested problems will be announced on the course website. Students are encouraged to attempt to solve all of these problems in a timely manner, and ask the instructors about the ones that they cannot solve.

<u>Attendance</u>: Attendance will not be recorded. However you are strongly recommended to follow the lectures. In case of a scheduling conflict with another course, you may attend an alternative section that fits to your timetable.

NA Policy: A student who misses all exams will receive a grade of NA for the course.

<u>Make-up Policy:</u> In order to be eligible to enter a make-up examination for a missed examination, a student should have a documented or verifiable, and officially acceptable excuse. A student cannot get make-up examinations for two missed exams. The make-up examination for all exams will be after the final exam, and will include all topics.

Instructor	Lecture Times and Places	Instructor e-mail,
		Office (Math building), office phone
S1. Yıldıray Ozan	Tue 8:40-10:30 (YP-A1),	ozan@metu.edu.tr
	Thu 10:40-12:30 (YP-A3)	217, (312) 210 5373
S2. Mohan Lal Bhupal	Tue 8:40-10:30 (YP-A4),	bhupal@metu.edu.tr
	Thu 10:40-12:30 (YP-A4)	238, +90 (312) 210-5378
S3. Özcan Yazıcı	Tue 13:40-15:30 (U3)	oyazici@metu.edu.tr
	Fri 8:40-10:30 (U3)	127, (312) 210 5387
S4. Kostyantyn Zheltukhin	Tue 13:40-15:30 (P2)	zheltukh@metu.edu.tr
	Fri 8:40-10:30 (P2)	137, (312) 210 5385
S5. Marat Akhmet	Tue 13:40-15:30 (YP-A2)	marat@metu.edu.tr
	Fri 8:40-10:30 (YP-A1)	121, (312) 210 5355
S6. Haydar Alıcı	Tue 13:40-15:30 (U1)	ahaydar@metu.edu.tr
	Fri 8:40-10:30 (U1)	225, (312)210 2976
S7. Haydar Alıcı	Tue 15:40-17:30 (U3)	ahaydar@metu.edu.tr
	Thu 8:40-10:30 (U3)	225, (312)210 2976
S8. (closed)		
S9. Ahmet İrfan Seven	Wed 15:40-17:30 (YP-A2)	aseven@metu.edu.tr
	Fri 10:40-12:30 (YP-A1)	226, (312) 210 5391

Important Dates:

- September 29: Classes begin
- October 6-10: Add-drop and advisor approvals
- October 29: Republic Day (28 October Tuesday is a half day holiday and 29 October Wednesday is a full day holiday)
- **November 10:** Commemoration of Atatürk (Monday)
- **December 1-7:** Course withdrawal applications
- **January 1:** New Year's Day (Thursday)
- **January 2:** Last day of classes
- January 5-17: Final exam period
- **January 26:** The announcement of letter grades

Course Schedule:

The table below is a rough guideline for the content of course lectures. Instructors may reorder their lectures as necessary/desired. Section and page numbers below are from the textbook, *Elementary Differential Equations* and *Boundary Value Problems*, Boyce and DiPrima, 10th ed., 2010.

Week 1: Sep.29-Oct.3	1	 §1.1, §1.3: Introduction, Direction Fields Chapter 2. First Order Differential Equations §2.2: Separable equations (also homogeneous equations - see p49 #30).
	2	§2.1: Linear equations; Method of integrating factors.

Oct.6-10 4 \$2.4: Differences between linear and nonlinear equations 5 \$2.6: Exact equations and integrating factors. Chapter 7. Systems of First Order Linear Equations 87.2: Review of matrices. Week 4: Oct.20-24 87.8 Systems of linear algebraic equations; Linear independence, eigenvalues, eigenvectors. Week 5: Oct.27-Oct.31 9 \$7.4: Basic theory of systems of first order linear equations. 87.5: Homogeneous linear systems with constant coefficients. 87.6: Complex eigenvalues. 87.7: Fundamental matrices. 87.8: Repeated eigenvalues. 12 \$7.9: Nonhomogeneous linear systems (variation of parameters only). Chapter 4. Higher Order Linear Equations 84.1: General theory of nh order linear equations 85.1:	Week 2:	3	§2.3: Modeling with first order equations		
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