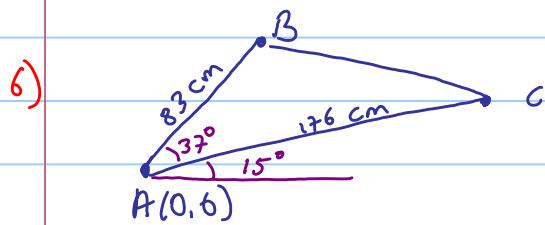


- 1) Prove that  $\int_0^1 \frac{\ln(1+x)}{x} dx = \sum_{n=1}^{\infty} \frac{(-1)^{n+1}}{n^2}$  and determine how many terms should be used to approximate this sum with an error  $< \frac{1}{120}$
- 2) Approximate  $\int_0^1 \cos(x^3) dx$  with an error  $< 5 \times 10^{-4}$
- 3) Find Maclaurin series of  $\frac{1-e^{2x}}{x}$  &  $\ln(e+x^2)$  and find their R/I.
- 4) Find the area of the triangle with vertices  $P(1,1,0)$ ,  $Q(1,0,1)$  and  $R(0,1,1)$ .
- 5) Suppose that  $\vec{u} \cdot (\vec{v} \times \vec{w}) = 2$ . Find;  
 a)  $(\vec{u} \times \vec{v}) \cdot \vec{w}$    b)  $\vec{u} \cdot (\vec{w} \times \vec{v})$   
 c)  $\vec{v} \cdot (\vec{u} \times \vec{w})$    d)  $(\vec{u} \times \vec{v}) \cdot \vec{v}$



First  
Find coordinates of each vertex,  
then calculate the area of  $\triangle ABC$   
( $139.5, 657$ )

- 6) The point  $D(3,3)$  is midpoint of one of the sides of a triangle. If two vertices are at  $B(1,1)$  and  $C(2,4)$ , find the area of the triangle.
- 7) Find the distance between points with polar coordinates  $E(3, 16^\circ)$ ,  $F(5, 36^\circ)$
- 8) Find the projection of  $\vec{a} = \langle 1, 2, 3 \rangle$  onto  $\vec{b} = \langle 1, 4, 1 \rangle$
- 9) Given the points  $A=(1,3,7)$ ,  $B=(7,12,22)$ ,  $C(3,5,1)$  and  $D=(15,20,4)$ . Let  $X$  be point on  $[AB]$  s.t.  $\frac{|AX|}{|XB|} = \frac{1}{2}$  and  $Y$  be the point on  $[CD]$  s.t.  $\frac{|CY|}{|YD|} = \frac{2}{1}$ . Find the midpoint of  $[XY]$  ( $7, \frac{21}{2}, \frac{5}{2}$ )
- 10) Given the points  $A(4,8)$ ,  $B(1,3)$  and  $C(5,6)$ , Find the length of the altitude of the triangle  $ABC$  passing through the vertex  $A$  ( $\sqrt{5}$ )
- 11) Find all values of  $m$  for which the points  $A(2,3)$  and  $B(-3,5)$  are placed on the two different sides of the line  $2x-3y+m=0$ . ( $m \in (5, 21)$ )