

Student No: _____
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Time: April 27, 12:15
Duration: 15 min.
Weight: 10 points
Score: _____

MATH 118 - 2018 Spring
Section-24 Quiz-5

1. (5pts) Let $\vec{u} = (-1, 2, 1)$ and $\vec{v} = (3, 1, 1)$ be two vectors. Find the angle between \vec{u} and \vec{v} .
2. (5pts) Identify the surface represented by the equation

$$x^2 - y^2 + z^2 - 2x + 2y + 4z + 2 = 0.$$

Note: Show all your work as is done in the lectures.

ANSWER

$$\begin{aligned} 1. \quad \vec{u} \cdot \vec{v} &= (-1, 2, 1) \cdot (3, 1, 1) \\ &= -3 + 2 + 1 = 0 \end{aligned}$$

Thus, \vec{u} and \vec{v} are perpendicular
The angle is 90°

$$2. \quad x^2 - y^2 + z^2 - 2x + 2y + 4z + 2 = 0$$

$$\Leftrightarrow x^2 - 2x + 1 - (y^2 - 2y + 1) + z^2 + 4z + 4 = 2$$

$$\Leftrightarrow (x-1)^2 - (y-1)^2 + (z+2)^2 = 2$$

$$\Leftrightarrow \frac{(x-1)^2}{2} - \frac{(y-1)^2}{2} + \frac{(z+2)^2}{2} = 1$$

This is a hyperboloid of one sheet centered at $(1, 1, -2)$

